



ISBN: 978-979-028-799-0

# Trends and Challenges toward Asian Economic Community

# PROCEEDING



December 5th, 2015

Auditorium Prof. Slamet Dajono Gedung D1 Lt.3 FMIPA

Kampus Unesa Ketintang Jl. Ketintang, Surabaya Jawa Timur 60231

http://icerd.unesa.ac.id

# **Preface**

Dear all ICERD participants, welcome to Surabaya, Indonesia. Welcome also to Universitas Negeri Surabaya. We are very glad to have you all, to participate in this conference.

In celebrating its 51st anniversary, The State University of Surabaya/Universitas Negeri Surabaya, proudly presents "The 2015 Internasional Conference on Educational Research and Development". The conference is conduction to bring together diversed ideas of researchers, educators, lecturers, teachers, students, and those who have interests in research on education and its development as well as on science and technology.

We are very honored to have Prof. Dr. Muhammad Nuh, DEA (former Republic of Indonesia Minister of Education and Culture, 2009 – 2014), Prof. Dr. Muchlas Samani (Universitas Negeri Surabaya, Indonesia), Prof. Dr. Fou-Lai Lin (National Taiwan Normal University), Prof. Dr. Bill Atweh (Adjunct Professor of Curtin University, Australia, and visiting Professor at Philippines Normal University), and Prof. Dato' Abdul Rahman B. Abdul Aziz, Ph.D (Universiti Utara Malaysia), and Dr. Zeny Reyes (Philippines Normal University) as keynote and plenary speakers.

To all our sponsors for this conference, Bank Tabungan Negara (Universitas Negeri Surabaya branch) and Telkom Divre 5 Surabaya, our thanks are also for you.

On behalf of the Organizing Committee and Steering Committee, I wish you all a blessed and productive time in our ICERD conference. God bless you all.

December 1, 2015 Surabaya Arie Wardhono

# **Program Committee**

Rooselyna Ekawati Shofan Fiangga Luqman Hakim Rita Ismawati Muhammad Jacky Ibnu Febry Kurniawan Dimas Maulana Ali Mustofa Arinto Nugroho Didik Nurhadi Agus Ridwan Arie Wardhono The State University of Surabaya

# **Table of Contents**

Dormitory Teachers Education System: Improving the Education Quality of Students Teacher in Indonesia to Answer the Challenges of Asian Economics Community (AEC)	1
The Analysis of English Language Education Students' Basic Teaching Skills during Listening and Speaking Microteaching in Groups	14
Literature Research in Indonesia, Ecopsychology Perspective	23
Modiste: A Novel Method for Enhancing Video Streaming in E-learning	28
The Effect of Problem Based Learning Model for High School Student Geography Learning Outcomes	35
SIBI and BISINDO Which One is Better For Deaf and Mute People Education?	17
CLIL and Its Feasibility to be implemented in Indonesia towards ASEAN Economic Community Silfia Asningtias	56
âĂŸReform' Magazine: A Medium in Reforming Student-Author's Motivation In Writing English 5 Prima Beauty Kartikasari	57
Surabaya Hinterland Area Development In Asean Economic Community	63
Industrial Area Development in East Java	70
Utilizing Business Model Canvas (BMC) to Develop Innovative Analysis in Culinary Business	71
The English Presentation on Business Plan Delivered by Economics Student of Unesa (A Case Study)	72
The Role of "Ma'had Aly" in Building Students' Characters	87
Metacognitive Activity in Conjecturing Process in Problem Solving of pattern Generalization	91
The Analysis of Multimedia Elements in PowerPoint Presentation (A Study towards Student  Teachers of Economics Education)	)3
Develop Learning Equipment Using CTL (Contextual Teaching And Learning) Model Assisted By PhET Software	12
Synthesis Al-UiO-66-NH2 with Acetic Acid Modulator by Solvothermal Method	19
Improving Soft Skills by Applying Model Centered Learning the Students For Students to SMK Kartika 1 Surabaya Program Accounting Expertise	26

Short Movie as tools for Learning Sociology
Trends and Challenges of Integrated Mentoring Support for Novice Teachers' Professionalism: A Case Study of a "Lesson Study" Program in an Indonesian Secondary School
Optimizing the Existence of Micro, Small, Medium Business Entrepreneurs as the Central of Industry in Facing ASEAN Economic Community Based on Local Wisdom (Optimizing Micro, Small, Medium Business of Madura's Snacks Business)
Synthesis and Characterization UiO-66 and Sn-UiO-66 by Solvothermal Method
Some Contributing Factors to the Students' English Achievemenent
The Influence of Problem Based Learning Model to Geography Learning Output of Senior High School Students
Nutritional and Quality Analysis of Kelor (Moringa oliefera) Beverage
21st Century English Education: High Order Thinking Skills and Technology Support
Multicultural Learning Model
The Intercultural Sensitivity of Vocational High School English Teachers
The Influence of Group Investigation Learning Model towards the Learning Motivation of Geography Students in Senior High School
The Effect students' perceptions of teachers teaching style and student learning styles of student learning outcomes on economic subjects
The Study of Ruthenium Dyes Endowed with Alkyl Chain for DSSC Sensitizer
Teacher Performance Based on Stress and Organizational Commitment
Influence Perceived of Usefulness of Self-Efficacy With Attitude to Mediation Aplicom
Analysis on the Abality of Elementary School Student Who Had High Mathematics Ability in Making The Equation of Fractions
The Quality of the Production of Methyl Ester from Jatropha Curcas lin Using Catalyst of H2SO4 296  Muhaji Mangil
Development Material Teaching Subject of Introduction of Administration and Management in  University

Developing Instructional Program of Public Economic Subject Using Exelsa Moodle
Peer Response in an Indonesian EFL Writing Class: A Case Study
Use of Project Based Learning Model to Improve Creativity Class XI Subject to the Installation of Electricity 5 SMKN in Surabaya
Biology Teachers' Self Perception on Pedagogical Competence
A Critical Review of Empirical Research in Environmental Education
Toward a Bright Future of Socio-Political Trends in Literary and Cultural Studies in Asia: Its  Development and Impacts In Asian Educational Backgrounds
Facilitating Authentic Language Learning Through Theatrical Activities
"Let's Speak!": Utilizing Voxopop to Enhance Speaking Skill
Exploring Students' Use of Communication Strategies
Prosocial and Risk-Taking Level on Teaching Intentions in Remote Areas (A Study on Students of Elemantary School Teacher in East Java)
The Implementation of Metacognition-Based Information and Communication Technology (ICT) In Vocational Education
Zone of Promoted Action (ZPA) of Elementary School Teacher in Mathematics Learning
The Urgency of Gen Z Economic Education
Board Game as a Media to Increase Students' Speaking Skill
Developing Taxation Learning Model by Using Animated Media to Enhance Students'  Comprehension
"Let's Write a Caption!": Utilizing Instagram to Teach Generation Y
Social Studies Teacher Role in the Development of Pattern Learning System Facing AEC 2015 456  Jossapat Prijanto
Developing Language Games for Teaching English to the Eighth Grade Students of SMP Negeri 1 Tulungagung
A Proposed Syllabus for Computer and Networking Technology Students of Vocational High School at Jember

Learning Model Talking Stick As An Effort to Improve Collaboration Students Office  Administration Education of Secretary Subjects
Thinking Process Statistics on Primary School Students in Resolving Issues Statistics
Theories of Moral Education And Implementation In Indonesia: Re-Energizing Cultural Identity and Addressing Future Challenges
Enhance The Student's Result Through The Implementation of Problem Based Learning In Making Man's Shirts Pattern Subject in Fashion Science Student at Surabaya State University 505  Imami Rahayu, Anneke Karyaningrum and Biyan Wilujeng
Developing Virtual Test as Alternative Assessment for Measure Student' Science Literacy
Actualization of Parenting Education Program to Encourage the Optimization of Non Formal  Education
What Have the Teachers Learnt from CLIL?
Socio-Economic Impact of Traditional Crude oil Mining to Traditional Mining Community in rural Districts Wonocolo Kedewan – Bojonegoro
Effectiveness Course Introduction to Accounting in the financial records in Accounting Education among Students in 2013
Student's Creative Reasoning in Solving Pattern Generalization Problem: A Case Study
Implementing Inquiry-Based Instruction In a Indonesian Snack and Beverage Management556  Ita Fatkhur Romadhoni Romadhoni, Dwi Kristiastuti and Siti Yuliana
Analyzing Student's Understanding the Relationship Between Quadrilateral at the Early Formal Stage
Teaching Speaking through rong-chang Website
Developing IELTS Curriculum for University Students: A Current Trend on Standardized Foreign  Language Testing
Environmental Approach with Science Kit Seqip to Enhancing Students' Scientific Process Skills,  Learning Motivation, and Cognitive Learning Outcomes
Curriculum Based Blended Learning Model to Improve Student Softskill in Higher Education 592  Nisaul Barokati Selirowangi and Nurdian Susilowati
"Enemies" at Our Home: The Threat to Indigenous Languages Seen from Language Use
Developing Instructional Design of Literary Appreciation Based on Reader Response Theory 610  Heny Subandiyah

Increase Ability Creative Economic Thinking Through
Students' Attitude towards Critical Thinking Practices in Classroom Discussion
Small Medium Enterprise (SME) Partnership Model Using the Triple Helix to Improve Competitiveness Towards Asean Economic Community
Learning to Write Short Story Using Mind Map Technique
Developing Update Portfolio as Authentic Assessment in Teaching Speaking for University Students: A Challenge to be Trending Lecturers
Material Conception, Development Strategy and Constraint in Implementing Civic Education  Curriculum
The Students Teacher Readiness in Implementing Economic Curriculum 2013 (Study of Self-Efficacy Theory)
Indicators of Conjecturing Process in Problem Solving of patterns Generalization
Inquiry-Based Integrated Science Education: The Application of Local Content Soil Washing Project to Improve Junior High School Students' Environmental Literacy
Students' Perception on the Benefits and Problems of Blended Learning
Neuroplasticity Concept in Teaching Elementary School Students: Preparing the 21st Century  Generation
Assistance Compilation Module and Lesson Plan of Craft and Entrepreneurship Subject to Produce Face Cream for Science Teachers High School and Vocational School in Kediri
Brand and Repurchase Intention
Fan Fiction in the Class
Modelling Student Mathematical Argumentation With Structural-Intuitive and Deductive  Warrant to Solve Mathematics Problem
Using Animation Clips to Improve the Listening Ability of the Tenth Grade Students Majoring in Animation
The Use of Digital Stories to Improve Students' Recount Writing Ability

# ANALYSIS ON THE ABILITY OF ELEMENTARY SCHOOL STUDENT WHO HAD HIGH MATHEMATICS ABILITY IN MAKING THE EQUATION OF FRACTIONS

Syarifatul Maf'ulah 1, Dwi Juniati 2, Tatag Yuli Eko Siswono 2

<sup>1</sup>STKIP PGRI Jombang, syarifatul.m@gmail.com

<sup>2</sup>UNIVERSITAS NEGERI SURABAYA (dwi\_juniati@yahoo.com, tatagyes@yahoo.com)

#### ABSTRACT

The purpose of this study was to analyze the ability of fifth grade elementary school student who had high mathematic ability in making the equation of fractions. This kind of research was qualitative by a student subject. Data collection was conducted by giving a test to the subject, continued by interviews. The next stage was data analysis, include reduce the data, presentate the data, conclusion and verificate the data. Subject was given a test containing an equation  $\frac{4}{5} - a = \frac{1}{4}$  as initial equation. Then, subject was asked to make an another equation as equivalent as initial one as much as possible. The result test indicated that subject able to make the eleven equations correctly. The following steps were (1) subject changed the initial equation element position; (2) subject referred on  $\frac{4}{5} - \frac{1}{4} = a$ , then changed both elements known to the another equivalent fraction; (3) subject changed the operan known at initial equation to the another equivalent fraction without changed the position of elements at initial equation; (4) subject referred on  $a + \frac{1}{4} = \frac{4}{5}$ , then changed both elements known to the another equivalent fraction; (5) subject changed the element position from initial equation, then added both elements with an element or an a.

Keywords: analysis, ability to make equation, fraction

#### I. INTRODUCTION

The research is inspired by Piaget's theory of reversibility. Reversibility means the person mental ability to change the mind purpose to the original point (Piaget via Slavin, 2008: 48). While (Krutetskii, 1976: 287) explains that reversibility is the person thinking to build up the reversible sides. Furthermore, Krutetskii identifies one of the categorized mathematics ability related to success in solving the problem, it is reversibility. On the other hand, student mathematics ability has the role in solving mathematical problem. It means that reversibility affects the student ability to solve the problem. Whereas problem solving is the learning mathematics focused. This is constructed by NCTM (2000: 52) that expands problem solving is the integral part of learning matematics. It is relevant with Soedjadi (1992: 33) states mathematics should be directed to develop the student future live transferable ability.

Reversibility is the person thinking ability to build up the reversible sides. It means that reversibility has two reversible ways, they are beginning side to the final one as the reached goal, and the final side returns to the beginning one. However, research focussed is how the student thinking ability from the beginning side to the final. The beginning side is the first equation test given. Then, subject asked to make many equations as equivalent as the beginning one. So the equation student made means the rearched goal.

The defined equation related to fractions and arithmetic operations. Fractons is on of the pre-requisites for understanding the subsequent and the intertwined materials of fractions concept. If student do not understand the basic, student will difficulty in studying further. Research subject is the fifth grade of elementary school student by considering the fractions is the first time material given at elementary school. In addition, Piaget states the ability of building the two-way relation develop in concrete operastional stage, it is about 7 to 11 years old. It means reversibility begins on elementary school student. But focus of research subject is student who had high mathematics by considering the result of research is used as basic by the teacher to teach fractions and arithmetic operations. In expectation is the ability the other student can be same or equal with ability of student who had high mathematics especially fraction and arithmatics operation materials. Based on the descriptions, researcher interested analyzing the elementary student ability in making fractions.

#### II. RESEARCH METHOD

# Research Design

This study purposed analyzing the elementary school student ability in making fractions. Therefore, this is a descriptive qualitative research. Researcher gave a test to the subject, then researcher conducted interview to the suject for comprehending about the things of uncovered test yet. Furthermore, the result data analyzed based on the framework established in theoritical study.

#### Research Subject

Research subject was the fifth grade of elemetary school student who is capable in high mathematic. High mathematic information was obtained by mathematic test and consultation with the teacher

#### Research Instrument

The main instrument is the researcher herself. While supporting instrument are as follows:

- Test used to obtain the data about subject's ability delineation in making equation. A test
  contains an equation then subject was asked to make as many as another equivalent equation.
- Interview guideline in this study is semi-structured or opened. Subject was interviewed based on the work result

#### Research Procedure

Research procedure consists of three stages described by following:

#### Preparation Stage

The research preparation stage examines theory in making equation's ability refers to part of reversibility characteristic.

### 2. Implementation Stage

The research implementation stage selectes the subject. Furthermore, researcher give a test to the subject, then followed by interviewed based on the work result.

# 3. Analysis Stage

The research analysis stage analyzes the data and report writing.

## **Data Analysis Technique**

Result data was analyzed with references to (i) the equation subject made number (ii) subject's way in making each the beginning equivalent equation. Analysis conducted after finishing the interview. Then data analysis conducted by following step: (1) data reduction; (2) data exploring; (3) drawing conclusion.

#### III. RESULT AND DISCUSSION

Before research was conducted, researcher choose the subject previously, it is fifth grade of elementary student of MIN Kauman Jombang. Furthermore, researcher conduted the research and analyzed the result data

### **Data Analysis Finding and Discussion**

#### 1. Test result

A test was given by the researcher such as the following:

TEST (30 minutes)
Given the following form:
Form: "
$$\frac{4}{5} - a = \frac{1}{4}$$
"
Rewrite the above from to the "another similar form" as much as possible

Fig. 1. Test Instrument

The followings are the the result subject in making the equation

Table 1 : Subject Equation Made

Equation Code	Subject Equation Made
P1	$\frac{4}{5} = \frac{1}{4} = 0$
P2	$a + \frac{1}{4} = \frac{4}{5}$
Р3	$\frac{8}{10} - \frac{2}{8} = \alpha$
P4	$\frac{8}{10}$ - $\alpha = \frac{1}{4}$
P5	$\frac{4}{5} - \frac{2}{8} = \alpha$
Р6	$\alpha + \frac{3}{12} = \frac{6}{10}$
P7	$\frac{1}{4} + \frac{1}{4} + \alpha - \frac{4}{5} = \frac{1}{4}$
P8	\frac{4}{5} - a - \frac{1}{4} + a = a
Р9	$\frac{1}{4} + \frac{4}{5} = \frac{4}{5} - \alpha + \frac{4}{5}$
P10	$\frac{4}{5} + a = a + a + \frac{1}{4}$
P11	$\frac{1}{4} + \alpha = \frac{4}{5}$

Based on the test result, known the subject has made 10 the beginning equivalent equation.

While subject way in making the beginning equivalent equation was obtained from interview. The followings are the subject way in making each equation

Table 2: Subject Way in Making Each Equation

Equation Code	Equation Subject Made	Equation Making Way
P1	4 = 1 = a	The beginning equation was $\frac{4}{5}$ — $a = \frac{1}{4}$ subject made P1 by moving $\frac{1}{4}$ elements to the right side and moving a to left side, obtained $\frac{4}{5}$ — $\frac{1}{4} = a$ as P1
P2	a + 1 4 5	The beginning equation was $\frac{4}{5}$ — $a = \frac{1}{4}$ . Subject made P2 by moving a side. It should be obtained $\frac{4}{5} = \frac{1}{4} + a$ , but subject wrote in $a + \frac{1}{4} = \frac{4}{5}$ form by reasoning there were an equal sign "=", so $\frac{4}{5} = \frac{1}{4} + a = a + \frac{1}{4} = \frac{4}{5}$ . Thus, obtained $a + \frac{1}{4} = \frac{4}{5}$ as P2.
Р3	$\frac{8}{10} \cdot \frac{2}{8} = a$	The beginning equation was $\frac{4}{5}$ — $a = \frac{1}{4}$ . Subject made P3 in reference to P1, it was $\frac{4}{5} - \frac{1}{4} = a$ because of the beginning equation made. Then subject changed both of known elements on $\frac{4}{5} - \frac{1}{4} = a$ to an another equivalent fraction. It changed $\frac{4}{5}$ into $\frac{8}{10}$ and $\frac{1}{4}$ into $\frac{2}{8}$ obtained $\frac{8}{10} - \frac{2}{8} = a$ as P3

The beginning equation was $\frac{4}{5}$ and $\frac{1}{4}$ . Subject made P4 by changing the side knowed on beginning equation to an another equivalent fraction. It changed $\frac{4}{5}$ as $\frac{8}{10}$ obtained $\frac{8}{10} - a = \frac{1}{4}$ as P4  The beginning equation to an another equivalent fraction. It changed $\frac{4}{5}$ as $\frac{8}{10}$ obtained $\frac{8}{10} - a = \frac{1}{4}$ as P4  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P5 in reference on P1, it was $\frac{4}{5} - \frac{1}{4} = a$ by reasoning P1 the beginning equation made. Then subject changed one of the element known by $\frac{4}{5} - \frac{1}{4} = a$ into an another equivalent fraction. It changed $\frac{1}{4}$ into $\frac{2}{6}$ obtained $\frac{4}{5} - \frac{2}{8} = a$ as P5.  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P6 in reference on P2, it was $a + \frac{1}{4} = \frac{4}{5}$ . Then it changed both of elements known by P2 into anan another equivalent fraction. It changed $\frac{4}{5}$ into $\frac{8}{10}$ and changed $\frac{1}{4}$ into $\frac{3}{12}$ obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.  P7  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained $a = \frac{1}{4}$ . Then added the			
P5 $\frac{4}{5} = \frac{2}{8} \text{ Subject made P4 by}$ changing the side knowed on beginning equation to an another equivalent fraction. It changed $\frac{4}{5}$ as $\frac{8}{10}$ obtained $\frac{8}{10} - a = \frac{1}{4}$ as P4  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P5 in reference on P1, it was $\frac{4}{5} - \frac{1}{4} = a$ by reasoning P1 the beginning equation made. Then subject changed one of the element known by $\frac{4}{5} - \frac{1}{4} = a$ into an another equivalent fraction. It changed $\frac{1}{4}$ into $\frac{2}{8}$ obtained $\frac{4}{5} - \frac{2}{8} = a$ as P5.  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P6 in reference on P2, it was $a + \frac{1}{4} = \frac{4}{5}$ . Then it changed both of elements known by P2 into anan another equivalent fraction. It changed $\frac{4}{5}$ into $\frac{8}{10}$ and $\frac{4}{5}$ into $\frac{8}{10}$ and $\frac{4}{5}$ into $\frac{8}{10}$ and $\frac{4}{5}$ into $\frac{8}{10}$ into $\frac{4}{5}$ into $\frac{8}{10}$ into $\frac{4}{5}$ into $\frac{8}{10}$ into $\frac{4}{5}$ into $\frac{8}{5}$ int	D4	8 - 0 = 1	The beginning equation was $\frac{4}{5}$ –
beginning equation to an another equivalent fraction. It changed $\frac{4}{5}$ as $\frac{8}{10}$ obtained $\frac{8}{10} - a = \frac{1}{4}$ as P4  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P5 in reference on P1, it was $\frac{4}{5} - \frac{1}{4} = a$ by reasoning P1 the beginning equation made. Then subject changed one of the element known by $\frac{4}{5} - \frac{1}{4} = a$ into an another equivalent fraction. It changed $\frac{1}{4}$ into $\frac{2}{8}$ obtained $\frac{4}{5} - \frac{2}{8} = a$ as P5.  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P6 in reference on P2, it was $a + \frac{1}{4} = \frac{4}{5}$ . Then it changed both of elements known by P2 into anan another equivalent fraction. It changed $\frac{4}{5}$ into $\frac{8}{10}$ and changed $\frac{1}{4}$ into $\frac{3}{12}$ obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained	F4	10 4	$a = \frac{1}{4}$ . Subject made P4 by
P5 $\frac{4}{5} - \frac{2}{8} = \frac{3}{8}$ The beginning equation was $\frac{4}{5} - \frac{1}{4} = a$ By reasoning P1 the beginning equation and the requivalent fraction. It changed $\frac{4}{5} - \frac{1}{4} = a$ By reasoning P1 the beginning equation made. Then subject changed one of the element known by $\frac{4}{5} - \frac{1}{4} = a$ into an another equivalent fraction. It changed $\frac{1}{4}$ into $\frac{2}{8}$ obtained $\frac{4}{5} - \frac{2}{8} = a$ as P5.  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P6 in reference on P2, it was $a + \frac{1}{4} = \frac{4}{5}$ . Then it changed both of elements known by P2 into an an another equivalent fraction. It changed $\frac{4}{5} = \frac{1}{10} = \frac{1}{10}$			changing the side knowed on
P5 $\frac{4}{5} - \frac{2}{8} = \frac{3}{4}$ The beginning equation was $\frac{4}{5} - \frac{1}{4} = a$ The beginning equation was $\frac{4}{5} - \frac{1}{4} = a$ The beginning equation was $\frac{4}{5} - \frac{1}{4} = a$ by reasoning P1 the beginning equation made. Then subject changed one of the element known by $\frac{4}{5} - \frac{1}{4} = a$ into an another equivalent fraction. It changed $\frac{1}{4}$ into $\frac{2}{8}$ obtained $\frac{4}{5} - \frac{2}{8} = a$ as P5.  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P6 in reference on P2, it was $a + \frac{1}{4} = \frac{4}{5}$ . Then it changed both of elements known by P2 into anan another equivalent fraction. It changed $\frac{4}{5}$ into $\frac{8}{10}$ and changed $\frac{1}{4}$ into $\frac{3}{12}$ obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.  P7  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained	16"		beginning equation to an another
P5 $\frac{4}{5} - \frac{2}{8}$ The beginning equation was $\frac{4}{5} - \frac{1}{4} = a$ $a = \frac{1}{4}$ . Subject made P5 in  reference on P1, it was $\frac{4}{5} - \frac{1}{4} = a$ by reasoning P1 the beginning  equation made. Then subject  changed one of the element  known by $\frac{4}{5} - \frac{1}{4} = a$ into an  another equivalent fraction. It  changed $\frac{1}{4}$ into $\frac{2}{8}$ obtained $\frac{4}{5} - \frac{2}{8} = a$ $a \approx P5$ .  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P6 in  reference on P2, it was $a + \frac{1}{4} = \frac{4}{5}$ .  Then it changed both of elements  known by P2 into anan another  equivalent fraction. It changed $\frac{4}{5}$ into $\frac{8}{10}$ and changed $\frac{4}{1}$ into $\frac{3}{12}$ obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.  P7 $\frac{1}{4} + \frac{1}{4} + a - \frac{4}{5} = \frac{1}{4}$ . The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P7 by  moving the a and $\frac{4}{5}$ side, obtained			equivalent fraction. It changed $\frac{4}{5}$
P5 $a = \frac{1}{4}$ . Subject made P5 in reference on P1, it was $\frac{4}{5} - \frac{1}{4} = a$ by reasoning P1 the beginning equation made. Then subject changed one of the element known by $\frac{4}{5} - \frac{1}{4} = a$ into an another equivalent fraction. It changed $\frac{1}{4}$ into $\frac{2}{8}$ obtained $\frac{4}{5} - \frac{2}{8} = a$ as P5.  P6 $a = \frac{1}{4}$ . Subject made P6 in reference on P2, it was $a + \frac{1}{4} = \frac{4}{5}$ . Then it changed both of elements known by P2 into anan another equivalent fraction. It changed $\frac{4}{5}$ into $\frac{8}{10}$ and changed $\frac{1}{4}$ into $\frac{3}{12}$ obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.  P7 $a = \frac{1}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained	4; -	o <sup>6</sup>	as $\frac{8}{10}$ obtained $\frac{8}{10} - a = \frac{1}{4}$ as P4
$a = \frac{2}{4}. \text{ Subject made P5 in}$ $reference \text{ on P1, it was } \frac{4}{5} - \frac{1}{4} = a$ by reasoning P1 the beginning equation made. Then subject changed one of the element known by $\frac{4}{5} - \frac{1}{4} = a$ into an another equivalent fraction. It $changed \frac{1}{4} \text{ into } \frac{2}{8} \text{ obtained } \frac{4}{5} - \frac{2}{8} = a$ $a \text{ as P5.}$ The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P6 in $reference \text{ on P2, it was } a + \frac{1}{4} = \frac{4}{5}.$ Then it changed both of elements known by P2 into anan another equivalent fraction. It changed $\frac{4}{5}$ into $\frac{8}{10}$ and changed $\frac{1}{4}$ into $\frac{3}{12}$ obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.  P7 $\frac{1}{4} + \frac{1}{4} + a - \frac{4}{5} = \frac{1}{4}.$ The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained		4-2 3 0	The beginning equation was $\frac{4}{5}$ –
by reasoning P1 the beginning equation made. Then subject changed one of the element known by $\frac{4}{5} - \frac{1}{4} = a$ into an another equivalent fraction. It changed $\frac{1}{4}$ into $\frac{2}{8}$ obtained $\frac{4}{5} - \frac{2}{8} = a$ as P5.  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P6 in reference on P2, it was $a + \frac{1}{4} = \frac{4}{5}$ . Then it changed both of elements known by P2 into anan another equivalent fraction. It changed $\frac{4}{5}$ into $\frac{8}{10}$ and changed $\frac{1}{4}$ into $\frac{3}{12}$ obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.  P7 $\frac{1}{4} + \frac{1}{4} + 0 - \frac{4}{5} = \frac{1}{4}$ The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained	P5	5 8	$a = \frac{1}{4}$ . Subject made P5 in
equation made. Then subject changed one of the element known by $\frac{4}{5} - \frac{1}{4} = a$ into an another equivalent fraction. It changed $\frac{1}{4}$ into $\frac{2}{8}$ obtained $\frac{4}{5} - \frac{2}{8} = a$ as P5.  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P6 in reference on P2, it was $a + \frac{1}{4} = \frac{4}{5}$ . Then it changed both of elements known by P2 into anan another equivalent fraction. It changed $\frac{4}{5}$ into $\frac{8}{10}$ and changed $\frac{1}{4}$ into $\frac{3}{12}$ obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.  P7 $\frac{1}{4} + \frac{1}{4} + 0 - \frac{4}{5} = \frac{1}{4}$ The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained			reference on P1, it was $\frac{4}{5} - \frac{1}{4} = a$
changed one of the element known by $\frac{4}{5} - \frac{1}{4} = a$ into an another equivalent fraction. It changed $\frac{1}{4}$ into $\frac{2}{8}$ obtained $\frac{4}{5} - \frac{2}{8} = a$ as P5.  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P6 in reference on P2, it was $a + \frac{1}{4} = \frac{4}{5}$ . Then it changed both of elements known by P2 into anan another equivalent fraction. It changed $\frac{4}{5}$ into $\frac{8}{10}$ and changed $\frac{1}{4}$ into $\frac{3}{12}$ obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained			by reasoning P1 the beginning
known by $\frac{4}{5} - \frac{1}{4} = a$ into an another equivalent fraction. It changed $\frac{1}{4}$ into $\frac{2}{8}$ obtained $\frac{4}{5} - \frac{2}{8} = a$ as P5.  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P6 in reference on P2, it was $a + \frac{1}{4} = \frac{4}{5}$ . Then it changed both of elements known by P2 into anan another equivalent fraction. It changed $\frac{4}{5}$ into $\frac{8}{10}$ and changed $\frac{1}{4}$ into $\frac{3}{12}$ obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.  P7 $\frac{1}{4} + \frac{1}{4} + a - \frac{4}{5} = \frac{1}{4}$ The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained			equation made. Then subject
another equivalent fraction. It changed $\frac{1}{4}$ into $\frac{2}{8}$ obtained $\frac{4}{5} - \frac{2}{8} = a$ as P5.  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P6 in reference on P2, it was $a + \frac{1}{4} = \frac{4}{5}$ . Then it changed both of elements known by P2 into anan another equivalent fraction. It changed $\frac{4}{5}$ into $\frac{8}{10}$ and changed $\frac{1}{4}$ into $\frac{3}{12}$ obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.  P7  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained			changed one of the element
changed $\frac{1}{4}$ into $\frac{2}{8}$ obtained $\frac{4}{5} - \frac{2}{8} = a$ as P5.  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P6 in reference on P2, it was $a + \frac{1}{4} = \frac{4}{5}$ . Then it changed both of elements known by P2 into anan another equivalent fraction. It changed $\frac{4}{5}$ into $\frac{8}{10}$ and changed $\frac{1}{4}$ into $\frac{3}{12}$ obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.  P7  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained			known by $\frac{4}{5} - \frac{1}{4} = a$ into an
P6 $ \begin{array}{c} a \text{ as P5.} \\ \hline A + \frac{3}{12} = \frac{6}{10} \\ \hline A + \frac{3}{12} = \frac{6}{10} \end{array} $ The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P6 in reference on P2, it was $a + \frac{1}{4} = \frac{4}{5}$ .  Then it changed both of elements known by P2 into anan another equivalent fraction. It changed $\frac{4}{5}$ into $\frac{8}{10}$ and changed $\frac{1}{4}$ into $\frac{3}{12}$ obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.  P7 $ \begin{array}{c} 1 + \frac{1}{4} + \Delta - \frac{4}{5} = \frac{1}{4} \\ \hline \end{array} $ The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained			another equivalent fraction. It
The beginning equation was $\frac{4}{5}$ - $a = \frac{1}{4}$ . Subject made P6 in reference on P2, it was $a + \frac{1}{4} = \frac{4}{5}$ . Then it changed both of elements known by P2 into anan another equivalent fraction. It changed $\frac{4}{5}$ into $\frac{8}{10}$ and changed $\frac{1}{4}$ into $\frac{3}{12}$ obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.  P7  The beginning equation was $\frac{4}{5}$ - $a = \frac{1}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained			changed $\frac{1}{4}$ into $\frac{2}{8}$ obtained $\frac{4}{5} - \frac{2}{8} =$
P6 $a = \frac{1}{4}. \text{ Subject made P6 in}$ reference on P2, it was $a + \frac{1}{4} = \frac{4}{5}$ . Then it changed both of elements known by P2 into anan another equivalent fraction. It changed $\frac{4}{5}$ into $\frac{8}{10}$ and changed $\frac{1}{4}$ into $\frac{3}{12}$ obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.  P7 $\frac{1}{4} + \frac{1}{4} + \alpha - \frac{4}{5} = \frac{1}{4}.$ The beginning equation was $\frac{4}{5} - \alpha = \frac{1}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained			a as P5.
$a = \frac{1}{4}. \text{ Subject made P6 in}$ $reference on P2, \text{ it was } a + \frac{1}{4} = \frac{4}{5}.$ Then it changed both of elements known by P2 into anan another equivalent fraction. It changed $\frac{4}{5}$ into $\frac{8}{10}$ and changed $\frac{1}{4}$ into $\frac{3}{12}$ obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.  P7 $\frac{1}{4} + \frac{1}{4} + a - \frac{4}{5} = \frac{1}{4}.$ The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained	D.C.	$\alpha + \frac{3}{2} = \frac{6}{2}$	The beginning equation was $\frac{4}{5}$ —
Then it changed both of elements known by P2 into anan another equivalent fraction. It changed $\frac{4}{5}$ into $\frac{8}{10}$ and changed $\frac{1}{4}$ into $\frac{3}{12}$ obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.  P7  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained	Po	12 10	$a = \frac{1}{4}$ . Subject made P6 in
known by P2 into anan another equivalent fraction. It changed $\frac{4}{5}$ into $\frac{8}{10}$ and changed $\frac{1}{4}$ into $\frac{3}{12}$ obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.  P7  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained	-		reference on P2, it was $a + \frac{1}{4} = \frac{4}{5}$ .
equivalent fraction. It changed $\frac{4}{5}$ into $\frac{8}{10}$ and changed $\frac{1}{4}$ into $\frac{3}{12}$ obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.  P7  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained			Then it changed both of elements
into $\frac{8}{10}$ and changed $\frac{1}{4}$ into $\frac{3}{12}$ obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.  P7  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained			known by P2 into anan another
obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.  P7  The beginning equation was $\frac{4}{5}$ — $a = \frac{1}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained			equivalent fraction. It changed $\frac{4}{5}$
P7 $\frac{1}{4} + \frac{1}{4} + \alpha - \frac{4}{5} = \frac{1}{4}$ The beginning equation was $\frac{4}{5}$ — $a = \frac{1}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained			into $\frac{8}{10}$ and changed $\frac{1}{4}$ into $\frac{3}{12}$
P7 $4 + 4 + 5 = \frac{1}{4}$ Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained			obtained $a + \frac{3}{12} = \frac{8}{10}$ as P6.
$a = \frac{2}{4}$ . Subject made P7 by moving the a and $\frac{4}{5}$ side, obtained		1 + + + 0 - 4 = 1	The beginning equation was $\frac{4}{5}$
	P7	4 4 5 4	$a = \frac{1}{4}$ . Subject made P7 by
$0 = \frac{1}{4} + a - \frac{4}{5}$ . Then added the			moving the a and $\frac{4}{5}$ side, obtained
			$0 = \frac{1}{4} + a - \frac{4}{5}$ . Then added the

sides of $0 = \frac{1}{4} + a - \frac{4}{5}$ with $\frac{1}{4}$ .  Obtained $\frac{1}{4} = \frac{1}{4} + a - \frac{4}{5} + \frac{1}{4}$ , but subject wrote $\frac{1}{4} + a - \frac{4}{5} + \frac{1}{4}$ , but subject wrote $\frac{1}{4} + a - \frac{4}{5} + \frac{1}{4}$ , but subject wrote $\frac{1}{4} + a - \frac{4}{5} + \frac{1}{4}$ , but subject wrote $\frac{1}{4} + a - \frac{4}{5} + \frac{1}{4}$ , but subject wrote $\frac{1}{4} + a - \frac{4}{5} + \frac{1}{4}$ , but subject wrote $\frac{1}{4} + a - \frac{4}{5} + \frac{1}{4}$ , but subject wrote $\frac{4}{4} + a - \frac{4}{5} + \frac{1}{4}$ , but subject wrote $\frac{4}{5} - a - \frac{1}{4} + \frac{1}{4}$ subject made by moving the $\frac{1}{4}$ subject wrote $\frac{4}{5} - a - \frac{1}{4} = 0$ . Then added the sides of $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P9 by changing $\frac{4}{5} - a = \frac{1}{4}$ subject wrote $\frac{4}{5} - a = \frac{1}{4}$ same as $\frac{1}{4} = \frac{4}{5} - a$ . Then added the sides of $\frac{1}{4} = \frac{4}{5} - a$ . Then added the sides of $\frac{1}{4} = \frac{4}{5} - a$ . Then added the sides of $\frac{1}{4} = \frac{4}{5} - a$ . Then added the sides of $\frac{1}{4} = \frac{4}{5} - a$ . Then added the sides of $\frac{1}{4} = \frac{4}{5} - a$ . Then added the sides of $\frac{1}{4} = \frac{4}{5} - a$ . Subject made P10 by moving the a side, obtained $\frac{4}{5} = a + \frac{1}{4}$ . Then operated the sides of $\frac{4}{5} = a + \frac{1}{4}$ with $a$ , obtained $\frac{4}{5} + a = a + a + \frac{1}{4}$ as P10  P11  P11  P11  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by wrote greater as a side, by the ball by the side of $\frac{4}{5} = a + \frac{1}{4}$ . Subject made P10 by writes the side of $\frac{4}{5} = a + \frac{1}{4}$ . Subject made P10 by writes the side of $\frac{4}{5} = a + \frac{1}{4}$ . Subject made P10 by writes the side of $\frac{4}{5} = a + \frac{1}{4}$ . Subject made P10 by			
subject wrote $\frac{1}{4} + a - \frac{4}{5} + \frac{1}{4}$ , $= \frac{1}{4}$ as P7  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made by moving the $\frac{1}{4}$ side, obtained $\frac{4}{5} - a - \frac{1}{4} = 0$ . Then added the sides of $\frac{4}{5} - a - \frac{1}{4} = 0$ with a, obtained $\frac{4}{5} - a - \frac{1}{4} = 0$ with a, obtained $\frac{4}{5} - a - \frac{1}{4} = 0$ with a, obtained $\frac{4}{5} - a - \frac{1}{4} + a = a$ as P8.  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P9 by changing $\frac{4}{5} - a = \frac{1}{4}$ form into $\frac{1}{4} = \frac{4}{5} - a$ by reasoning there was an equal sign "=", so $\frac{4}{5} - a = \frac{1}{4}$ same as $\frac{1}{4} = \frac{4}{5} - a$ . Then added the sides of $\frac{1}{4} = \frac{4}{5} - a$ . Then added the sides of $\frac{1}{4} = \frac{4}{5} - a$ . Then added the sides of $\frac{1}{4} = \frac{4}{5} - a$ . Then added the sides of $\frac{1}{4} = \frac{4}{5} - a$ . Then added the sides of $\frac{1}{4} = \frac{4}{5} - a$ . Subject made P10 by moving the a side, obtained $\frac{4}{5} = a + \frac{1}{4}$ . Then operated the sides of $\frac{4}{5} = a + \frac{1}{4}$ with a, obtained $\frac{4}{5} + a = a + a + \frac{1}{4}$ as P10  P11  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by			sides of $0 = \frac{1}{4} + a - \frac{4}{5}$ with $\frac{1}{4}$ .
P8 $\frac{4}{5} - \Delta - \frac{1}{4} + \Delta = \Delta$ The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made by moving the $\frac{1}{4}$ side, obtained $\frac{4}{5} - a - \frac{1}{4} = 0$ .  Then added the sides of $\frac{4}{5} - a - \frac{1}{4} = 0$ .  Then added the sides of $\frac{4}{5} - a - \frac{1}{4} = 0$ .  Then added the sides of $\frac{4}{5} - a - \frac{1}{4} + a = a$ as P8.  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P9 by changing $\frac{4}{5} - a = \frac{1}{4}$ form into $\frac{1}{4} = \frac{4}{5} - a$ by reasoning there was an equal sign "=", so $\frac{4}{5} - a = \frac{1}{4}$ same as $\frac{1}{4} = \frac{4}{5} - a$ . Then added the sides of $\frac{1}{4} = \frac{4}{5} - a$ with $\frac{4}{5}$ , obtained $\frac{1}{4} + \frac{4}{5} = \frac{4}{5} - a + \frac{4}{5}$ as P9  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by moving the a side, obtained $\frac{4}{5} = a + \frac{1}{4}$ . Then operated the sides of $\frac{4}{5} = a + \frac{1}{4}$ with $a$ , obtained $\frac{4}{5} + a = a + a + \frac{1}{4}$ as P10  P11  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by			Obtained $\frac{1}{4} = \frac{1}{4} + a - \frac{4}{5} + \frac{1}{4}$ , but
P8 $\frac{4}{5} - \Delta - \frac{1}{4} + \Delta = \Delta$ The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made by moving the $\frac{1}{4}$ side, obtained $\frac{4}{5} - a - \frac{1}{4} = 0$ .  Then added the sides of $\frac{4}{5} - a - \frac{1}{4} = 0$ with a, obtained $\frac{4}{5} - a - \frac{1}{4} + a = a$ as P8.  The beginning equation was $\frac{4}{5} - a = \frac{1}{4} + a = a$ as P8.  The beginning equation was $\frac{4}{5} - a = \frac{1}{4} + a = a$ as P8.  The beginning equation was $\frac{4}{5} - a = \frac{1}{4} + a = a$ as P8.  The beginning equation was $\frac{4}{5} - a = \frac{1}{4} + a = a$ by reasoning there was an equal sign "=", so $\frac{4}{5} - a = \frac{1}{4} + a = a$ as P9.  P10  The beginning equation was $\frac{4}{5} - a = \frac{1}{4} + a = a = a = a = a = a = a = a = a = a$		-	subject wrote $\frac{1}{4} + a - \frac{4}{5} + \frac{1}{4}, = \frac{1}{4}$
P8 $\frac{1}{5} - \Delta - \frac{1}{4} + \Delta = \Delta$ $a = \frac{1}{4} \text{ Subject made by moving the } \frac{1}{4} \text{ side, obtained } \frac{4}{5} - a - \frac{1}{4} = 0.$ Then added the sides of $\frac{4}{5} - a - \frac{1}{4} = 0$ with a, obtained $\frac{4}{5} - a - \frac{1}{4} = 0$ with a, obtained $\frac{4}{5} - a - \frac{1}{4} = 0$ with a, obtained $\frac{4}{5} - a - \frac{1}{4} = 0$ with a, obtained $\frac{4}{5} - a - \frac{1}{4} = 0$ with a, obtained $\frac{4}{5} - a - \frac{1}{4} = 0$ with a, obtained $\frac{4}{5} - a - \frac{1}{4} = 0$ with a, obtained $\frac{4}{5} - a - \frac{1}{4} = 0$ with a sides of $\frac{4}{5} - a - \frac{1}{4} = 0$ with a sides of $\frac{4}{5} - a - \frac{1}{4} = 0$ with a sides of $\frac{4}{5} - a - \frac{1}{4} = 0$ with a sides of $\frac{4}{5} - a - \frac{1}{4} = 0$ with a sides of $\frac{4}{5} - a - \frac{1}{4} = 0$ with a sides of $\frac{4}{5} - a - \frac{1}{4} = 0$ with a sides of $\frac{4}{5} - a - \frac{1}{4} = 0$ with a sides of $\frac{4}{5} - a - \frac{1}{4} = 0$ with a sides of $\frac{4}{5} - a - \frac{1}{4} = \frac{4}{5} - a + \frac{4}{5} = a + \frac$	W-		as P7
P10 $a = \frac{7}{4} \text{ Subject made by hoving}$ the $\frac{1}{4}$ side, obtained $\frac{4}{5} - a - \frac{1}{4} = 0$ . Then added the sides of $\frac{4}{5} - a - \frac{1}{4} = 0$ with a, obtained $\frac{4}{5} - a - \frac{1}{4} + a = a$ as P8.  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P9 by changing $\frac{4}{5} - a = \frac{1}{4}$ form into $\frac{1}{4} = \frac{4}{5} - a$ by reasoning there was an equal sign "=", so $\frac{4}{5} - a = \frac{1}{4}$ same as $\frac{1}{4} = \frac{4}{5} - a$ with $\frac{4}{5}$ ; obtained $\frac{1}{4} + \frac{4}{5} = \frac{4}{5} - a + \frac{4}{5}$ as P9  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by moving the a side, obtained $\frac{4}{5} = a + \frac{1}{4}$ . Then operated the sides of $\frac{4}{5} = a + \frac{1}{4}$ with a, obtained $\frac{4}{5} + a = a + a + \frac{1}{4}$ as P10  P11  The beginning equation was $\frac{4}{5} - a = a + a + \frac{1}{4}$ as P10  The beginning equation was $\frac{4}{5} - a = a + a + \frac{1}{4}$ as P10  The beginning equation was $\frac{4}{5} - a = a + a + \frac{1}{4}$ as P10  The beginning equation was $\frac{4}{5} - a = a + a + \frac{1}{4}$ as P10  The beginning equation was $\frac{4}{5} - a = a + a + a + \frac{1}{4}$ as P10  The beginning equation was $\frac{4}{5} - a = a + a + \frac{1}{4}$ as P10  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by		4-0-1+0.0	The beginning equation was $\frac{4}{5}$ –
Then added the sides of $\frac{4}{5} - a - \frac{1}{4} = 0$ with a, obtained $\frac{4}{5} - a - \frac{1}{4} + a = a$ as P8.  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P9 by changing $\frac{4}{5} - a = \frac{1}{4}$ form into $\frac{1}{4} = \frac{4}{5} - a$ by reasoning there was an equal sign "=", so $\frac{4}{5} - a = \frac{1}{4}$ same as $\frac{1}{4} = \frac{4}{5} - a$ . Then added the sides of $\frac{1}{4} = \frac{4}{5} - a$ with $\frac{4}{5}$ . obtained $\frac{1}{4} + \frac{4}{5} = \frac{4}{5} - a + \frac{4}{5}$ as P9  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by moving the a side, obtained $\frac{4}{5} = a + \frac{1}{4}$ . Then operated the sides of $\frac{4}{5} = a + \frac{1}{4}$ with $a$ , obtained $\frac{4}{5} + a = a + a + \frac{1}{4}$ as P10  The beginning equation was $\frac{4}{5} - a = a + a + \frac{1}{4}$ as P10  The beginning equation was $\frac{4}{5} - a = a + a + \frac{1}{4}$ as P10  The beginning equation was $\frac{4}{5} - a = a + a + \frac{1}{4}$ as P10  The beginning equation was $\frac{4}{5} - a = a + a + \frac{1}{4}$ as P10  The beginning equation was $\frac{4}{5} - a = a + a + \frac{1}{4}$ as P10  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by	P8	5 4 4 4 4	$a = \frac{1}{4}$ . Subject made by moving
P9 $\frac{1}{4} = 0 \text{ with a, obtained } \frac{4}{5} - a - \frac{1}{4} + a = a \text{ as P8.}$ The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P9 by changing $\frac{4}{5} - a = \frac{1}{4}$ form into $\frac{1}{4} = \frac{4}{5} - a$ by reasoning there was an equal sign "=", so $\frac{4}{5} - a = \frac{1}{4}$ same as $\frac{1}{4} = \frac{4}{5} - a$ . Then added the sides of $\frac{1}{4} = \frac{4}{5} - a$ with $\frac{4}{5}$ , obtained $\frac{1}{4} + \frac{4}{5} = \frac{4}{5} - a + \frac{4}{5}$ as P9  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by moving the a side, obtained $\frac{4}{5} = a + \frac{1}{4}$ . Then operated the sides of $\frac{4}{5} = a + \frac{1}{4}$ with $a$ , obtained $\frac{4}{5} + a = a + a + \frac{1}{4}$ as P10  P11  The beginning equation was $\frac{4}{5} - a = \frac{4}{5} - a + \frac{4}{5} + a = a + a + \frac{1}{4} + a = a + a + a + \frac{1}{4} + a = a + a + a + \frac{1}{4} + a = a + a + a + \frac{1}{4} + a = a + a + a + a + a + a + a + a + a$			the $\frac{1}{4}$ side, obtained $\frac{4}{5} - a - \frac{1}{4} = 0$ .
P9 $\frac{1}{4} + a = a \text{ as P8.}$ The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P9 by changing $\frac{4}{5} - a = \frac{1}{4}$ form into $\frac{1}{4} = \frac{4}{5} - a$ by reasoning there was an equal sign "=", so $\frac{4}{5} - a = \frac{1}{4}$ same as $\frac{1}{4} = \frac{4}{5} - a$ . Then added the sides of $\frac{1}{4} = \frac{4}{5} - a$ with $\frac{4}{5}$ , obtained $\frac{1}{4} + \frac{4}{5} = \frac{4}{5} - a + \frac{4}{5}$ as P9  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by moving the a side, obtained $\frac{4}{5} = a + \frac{1}{4}$ . Then operated the sides of $\frac{4}{5} = a + \frac{1}{4}$ with $a$ , obtained $\frac{4}{5} + a = a + a + \frac{1}{4}$ as P10  P11  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by			Then added the sides of $\frac{4}{5} - a -$
P9 $\frac{1}{4} + \frac{4}{5} = \frac{4}{5} - \Delta + \frac{4}{5}$ The beginning equation was $\frac{4}{5}$ — $a = \frac{1}{4}$ . Subject made P9 by changing $\frac{4}{5} - a = \frac{1}{4}$ form into $\frac{1}{4} = \frac{4}{5} - a$ by reasoning there was an equal sign "=", so $\frac{4}{5} - a = \frac{1}{4}$ same as $\frac{1}{4} = \frac{4}{5} - a$ . Then added the sides of $\frac{1}{4} = \frac{4}{5} - a$ with $\frac{4}{5}$ , obtained $\frac{1}{4} + \frac{4}{5} = \frac{4}{5} - a + \frac{4}{5}$ as P9  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by moving the a side, obtained $\frac{4}{5} = a + \frac{1}{4}$ . Then operated the sides of $\frac{4}{5} = a + \frac{1}{4}$ with a, obtained $\frac{4}{5} + a = a + a + \frac{1}{4}$ as P10  P11  The beginning equation was $\frac{4}{5} - a = \frac{4}{5}$ . The beginning equation was $\frac{4}{5} - a = a + a + \frac{1}{4}$ as P10  The beginning equation was $\frac{4}{5} - a = \frac{4}{5}$ . Subject made P10 by			$\frac{1}{4} = 0$ with a, obtained $\frac{4}{5} - a -$
P9 $a = \frac{1}{4}. \text{ Subject made P9 by}$ $changing \frac{4}{5} - a = \frac{1}{4} \text{ form into } \frac{1}{4} = \frac{4}{5} - a \text{ by reasoning there was an}$ $equal sign "=", so \frac{4}{5} - a = \frac{1}{4} \text{ same} as \frac{1}{4} = \frac{4}{5} - a. \text{ Then added the} sides of \frac{1}{4} = \frac{4}{5} - a \text{ with } \frac{4}{5}, obtained \frac{1}{4} + \frac{4}{5} = \frac{4}{5} - a + \frac{4}{5} \text{ as P9} The beginning equation was \frac{4}{5} - a = \frac{1}{4}. \text{ Subject made P10 by} moving the a side, obtained \frac{4}{5} = a + \frac{1}{4}. \text{ Then operated the sides of} \frac{4}{5} = a + \frac{1}{4}. \text{ With } a, \text{ obtained } \frac{4}{5} + a = a + a + \frac{1}{4}. \text{ as P10} P11 \frac{1}{4} + A = \frac{4}{5}. \text{ The beginning equation was } \frac{4}{5} - a = \frac{1}{4}. \text{ Subject made P10 by} \frac{1}{4} + A = \frac{4}{5}. \text{ Subject made P10 by}$			$\frac{1}{4} + a = a \text{ as P8}.$
P10 $a = \frac{1}{4}. \text{ Subject made P9 by}$ $changing \frac{4}{5} - a = \frac{1}{4} \text{ form into } \frac{1}{4} = \frac{4}{5} - a \text{ by reasoning there was an}$ $equal sign "=", so \frac{4}{5} - a = \frac{1}{4} \text{ same} as \frac{1}{4} = \frac{4}{5} - a. \text{ Then added the} sides of \frac{1}{4} = \frac{4}{5} - a \text{ with } \frac{4}{5}, obtained \frac{1}{4} + \frac{4}{5} = \frac{4}{5} - a + \frac{4}{5} \text{ as P9} The beginning equation was \frac{4}{5} - a = \frac{1}{4}. \text{ Subject made P10 by} moving the a side, obtained \frac{4}{5} = a + \frac{1}{4}. \text{ Then operated the sides of} \frac{4}{5} = a + \frac{1}{4}. \text{ With } a, \text{ obtained } \frac{4}{5} + a = a + a + \frac{1}{4}. \text{ as P10} P11 \frac{1}{4} + A = \frac{4}{5}. \text{ The beginning equation was } \frac{4}{5} - a = \frac{1}{4}. \text{ Subject made P10 by} \frac{1}{4} + A = \frac{4}{5}. \text{ Subject made P10 by}$		1+4=4-0+4	The beginning equation was $\frac{4}{5}$
P10 $\frac{4}{5} - a \text{ by reasoning there was an}$ equal sign "=", so $\frac{4}{5} - a = \frac{1}{4}$ same as $\frac{1}{4} = \frac{4}{5} - a$ . Then added the sides of $\frac{1}{4} = \frac{4}{5} - a$ with $\frac{4}{5}$ , obtained $\frac{1}{4} + \frac{4}{5} = \frac{4}{5} - a + \frac{4}{5}$ as P9  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by moving the a side, obtained $\frac{4}{5} = a + \frac{1}{4}$ . Then operated the sides of $\frac{4}{5} = a + \frac{1}{4} \text{ with } a, \text{ obtained } \frac{4}{5} + a = a + a + \frac{1}{4} \text{ as P10}$ P11 $\frac{1}{4} + a = \frac{4}{5}$ The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by	P9	7 5 5 5	$a = \frac{1}{4}$ . Subject made P9 by
equal sign "=", so $\frac{4}{5} - a = \frac{1}{4}$ same  as $\frac{1}{4} = \frac{4}{5} - a$ . Then added the  sides of $\frac{1}{4} = \frac{4}{5} - a$ with $\frac{4}{5}$ ,  obtained $\frac{1}{4} + \frac{4}{5} = \frac{4}{5} - a + \frac{4}{5}$ as P9  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by  moving the a side, obtained $\frac{4}{5} = a + \frac{1}{4}$ . Then operated the sides of $\frac{4}{5} = a + \frac{1}{4}$ with a, obtained $\frac{4}{5} + a = a + a + \frac{1}{4}$ as P10  P11 $\frac{1}{4} + a = \frac{4}{5}$ The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by			changing $\frac{4}{5} - a = \frac{1}{4}$ form into $\frac{1}{4} =$
P10 $as \frac{1}{4} = \frac{4}{5} - a. \text{ Then added the}$ $sides \text{ of } \frac{1}{4} = \frac{4}{5} - a \text{ with } \frac{4}{5},$ $obtained \frac{1}{4} + \frac{4}{5} = \frac{4}{5} - a + \frac{4}{5} \text{ as P9}$ $The beginning equation was \frac{4}{5} - a = \frac{1}{4}. \text{ Subject made P10 by}$ $moving the a side, obtained \frac{4}{5} = a + \frac{1}{4}. \text{ Then operated the sides of } \frac{4}{5} = a + \frac{1}{4}. \text{ with } a, \text{ obtained } \frac{4}{5} + a = a + a + \frac{1}{4}. \text{ as P10}$ $P11$ $P11$ $The beginning equation was \frac{4}{5} - a = \frac{1}{4}. \text{ Subject made P10 by}$ $The beginning equation was \frac{4}{5} - a = \frac{1}{4}. \text{ Subject made P10 by}$			$\frac{4}{5}$ – a by reasoning there was an
sides of $\frac{1}{4} = \frac{4}{5} - a$ with $\frac{4}{5}$ , obtained $\frac{1}{4} + \frac{4}{5} = \frac{4}{5} - a + \frac{4}{5}$ as P9  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by moving the a side, obtained $\frac{4}{5} = a + \frac{1}{4}$ . Then operated the sides of $\frac{4}{5} = a + \frac{1}{4}$ with $a$ , obtained $\frac{4}{5} + a = a + a + \frac{1}{4}$ as P10  P11  The beginning equation was $\frac{4}{5} - a = \frac{4}{5}$ . Subject made P10 by  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by			equal sign "=", so $\frac{4}{5} - a = \frac{1}{4}$ same
obtained $\frac{1}{4} + \frac{4}{5} = \frac{4}{5} - a + \frac{4}{5}$ as P9  The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by moving the a side, obtained $\frac{4}{5} = a + \frac{1}{4}$ . Then operated the sides of $\frac{4}{5} = a + \frac{1}{4}$ with $a$ , obtained $\frac{4}{5} + a = a + a + \frac{1}{4}$ as P10  P11 $\frac{1}{4} + a = \frac{4}{5}$ The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by			as $\frac{1}{4} = \frac{4}{5} - a$ . Then added the
P10  P10  The beginning equation was $\frac{4}{5}$ — $a = \frac{1}{4}$ . Subject made P10 by  moving the a side, obtained $\frac{4}{5}$ = $a + \frac{1}{4}$ . Then operated the sides of $\frac{4}{5} = a + \frac{1}{4}$ with $a$ , obtained $\frac{4}{5}$ + $a = a + a + \frac{1}{4}$ as P10  P11  The beginning equation was $\frac{4}{5}$ — $a = a + a + \frac{1}{4}$ as P10  The beginning equation was $\frac{4}{5}$ — $a = \frac{1}{4}$ . Subject made P10 by			sides of $\frac{1}{4} = \frac{4}{5} - a$ with $\frac{4}{5}$ ,
P10 $a = \frac{1}{4}. \text{ Subject made P10 by}$ $a = \frac{1}{4}. \text{ Subject made P10 by}$ $a = \frac{1}{4}. \text{ Then operated the sides of}$ $\frac{4}{5} = a + \frac{1}{4} \text{ with } a, \text{ obtained } \frac{4}{5} + a = a + a + \frac{1}{4} \text{ as P10}$ P11 $\frac{1}{4} + a = \frac{4}{5}$ The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by			obtained $\frac{1}{4} + \frac{4}{5} = \frac{4}{5} - a + \frac{4}{5}$ as P9
$a = \frac{1}{4}. \text{ Subject made P10 by}$ $a = \frac{1}{4}. \text{ Subject made P10 by}$ $a + \frac{1}{4}. \text{ Then operated the sides of}$ $\frac{4}{5} = a + \frac{1}{4} \text{ with } a, \text{ obtained } \frac{4}{5} + a = a + a + \frac{1}{4} \text{ as P10}$ P11 $\frac{1}{4} + a = \frac{4}{5}$ The beginning equation was $\frac{4}{5} - a = \frac{1}{4}$ . Subject made P10 by		4 +a = a+a+1	The beginning equation was $\frac{4}{5}$
$a + \frac{1}{4}. \text{ Then operated the sides of}$ $\frac{4}{5} = a + \frac{1}{4} \text{ with } a, \text{ obtained } \frac{4}{5} +$ $a = a + a + \frac{1}{4} \text{ as P10}$ P11 $\frac{1}{4} + a = \frac{4}{5}$ The beginning equation was $\frac{4}{5} -$ $a = \frac{1}{4}. \text{ Subject made P10 by}$	P10	4	$a = \frac{1}{4}$ . Subject made P10 by
$\frac{4}{5} = a + \frac{1}{4} \text{ with } a, \text{ obtained } \frac{4}{5} + $ $a = a + a + \frac{1}{4} \text{ as P10}$ P11 $\frac{1}{4} + \alpha = \frac{4}{5}$ The beginning equation was $\frac{4}{5} - $ $a = \frac{1}{4}$ . Subject made P10 by			moving the a side, obtained $\frac{4}{5}$ =
$a = a + a + \frac{1}{4} \text{ as P10}$ P11 $\frac{1}{4} + \alpha = \frac{4}{5}$ The beginning equation was $\frac{4}{5}$ — $a = \frac{1}{4}$ . Subject made P10 by			$a + \frac{1}{4}$ . Then operated the sides of
P11 $\frac{1}{4} + \alpha = \frac{4}{5}$ The beginning equation was $\frac{4}{5}$ = $\frac{1}{4}$ . Subject made P10 by			$\frac{4}{5} = a + \frac{1}{4}$ with a, obtained $\frac{4}{5}$ +
$\frac{1}{4} + \alpha = \frac{4}{5}$ The segmang equation was $\frac{1}{5}$ $a = \frac{1}{4}$ . Subject made P10 by			$a = a + a + \frac{1}{4} \text{ as P10}$
	PII	1 . 6 4	The beginning equation was $\frac{4}{5}$ —
marriage the egide. It shalled be		4 5	$a = \frac{1}{4}$ . Subject made P10 by
moving the a side. It should be		176.	moving the a side. It sholud be



Based on the table 2 above, obtained the descriptions of subject way in making the equation of fractions

- Subject made a new equation by the changing the side on beginning equation without changing these element to an another equivalent equation. At this category divided by two, they were as follows
  - a. Moving the  $\frac{1}{4}$  and a elements side

    The test beginning equation given was  $\frac{4}{5} a = \frac{1}{4}$ . Subject made a new equation by moving the  $\frac{1}{4}$  of right side and moving the a of left side. The subject equation made included P1 category was  $\frac{4}{5} \frac{1}{4} = a$ .
  - b. Moving the aelement side

    A test beginning equation given was  $\frac{4}{5} a = \frac{1}{4}$ . Subject made a new equation by moving the a element. The subject equation made included P2 category was  $\frac{1}{4} + a = \frac{4}{5}$ , and P11 category was  $a + \frac{1}{4} = \frac{4}{5}$ . But P11, subject also used the commutative to arithmetic, it was  $\frac{1}{4} + a = a + \frac{1}{4}$ .
- 2. Subject made a new equation in referenceon P1, it was  $\frac{4}{5} \frac{1}{4} = a$  by reasoning P1 made from the beginning equation. Then, subject changed the known sides of  $\frac{4}{5} \frac{1}{4} = a$  to an another equivalent equation. The subject equation made included P3 category was  $\frac{8}{10} \frac{2}{8} = a$  and P5 category was  $\frac{4}{5} \frac{2}{8} = a$ .
- 3. Subject made a new equation by changing the known side on beginning equation to an another equivalent equation. The subject equation made included P4 category was  $\frac{8}{10} a = \frac{1}{4}$ .
- 4. Subject made a new equation in reference on P2, it was  $a + \frac{1}{4} = \frac{4}{5}$ . Then, changed the known sides on P2 to an another equivalent equation. The subject equation made included P6 category  $a + \frac{3}{12} = \frac{8}{10}$ .

- Subject made a new equation by moving the side of beginning equation, then added the sides with the fractions. These category divided by two parts, they are as follows
  - a. Moving the one of beginning equation element then added those sides by fractions, the included category of equation was  $P8\frac{4}{5} a \frac{1}{4} + a = a$  and  $P10\frac{4}{5} + a = a + a + \frac{1}{4}$ .
  - b. Moving the beginning equation side elements then added those sides by fractions, the included category of equation was  $P7\frac{1}{4} + a \frac{4}{5} + \frac{1}{4} = \frac{1}{4}$ .
- 6. Subject made a new equation by moving one of these then added the sides by the fractions. The included category of equation was  $\frac{1}{4} + \frac{4}{5} = \frac{4}{5} a + \frac{4}{5}$ .

#### IV. CONCLUSION

Based on the result analysis obtained the conclusion about subject ability in making of equation. It was a subject making the eleven equivalent equations  $\frac{4}{5} - a = \frac{1}{4}$ . The subject way in making the beginning equivalent equation as follows

- 1. Subject only moved the beginning equation of element side.
- 2. Subject referenced at  $\frac{4}{5} \frac{1}{4} = a$ , then changed the known elements at  $\frac{4}{5} \frac{1}{4} = a$  to an another equivalent fractions
- 3. Subject changed the known position on beginning equation to an another equivalent fractions
- 4. Subject referenced at  $a + \frac{1}{4} = \frac{4}{5}$ , then changed the known sides on  $a + \frac{1}{4} = \frac{4}{5}$  to an another equivalent fractions
- 5. Subject moved the sides of beginning equation, then added the sides by fractions
- Subject moved one of the beginning equation sides then added those equation sides by the fractions

#### REFERENCES

- Krutetskii, V.A. The Psychology of Mathematical Abilities in Schoolchildren. Chicago: The University of Chicago Press (1976).
- National Council of Teachers of Mathematics (NCTM). Principles and standards for school mathematics. Reston, VA: NCTM (2000).
- Slavin, R. E. Psikologi Pendidikan: Teori dan Praktik. Jakarta: PT Indeks (2008).
- Soedjadi, R. Kiat Pendidikan Matematika di Indonesia: Konstatasi Keadaan Masa Kini Menuju Harapan Masa Depan. Jakarta: Dirjen Dikti Depdiknas (2000).